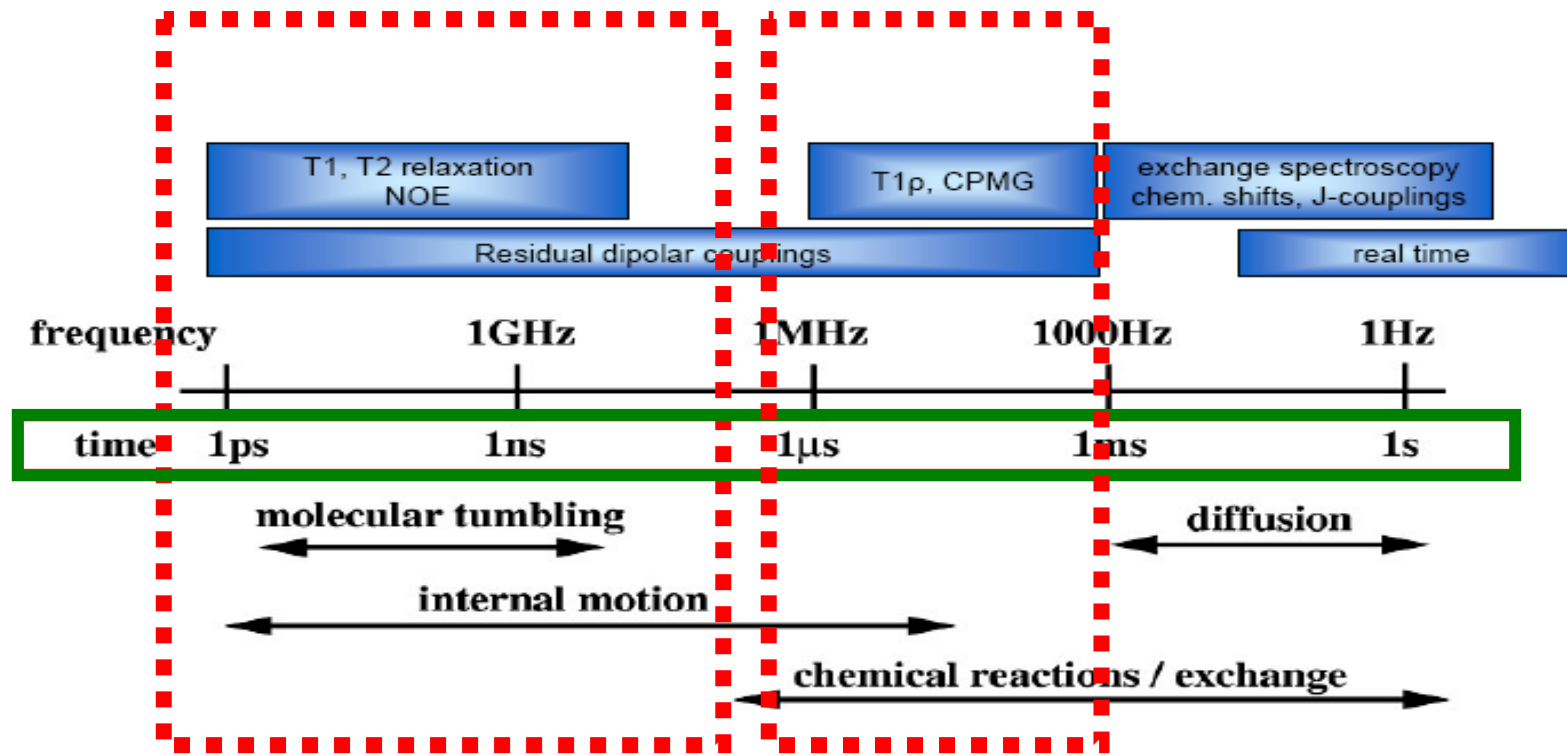


Overview of Protein Dynamics Studies Using NMR

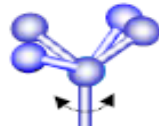
Chi-Fon Chang
HFNMRC
07.20.2010

NMR Time Scales for Protein Dynamics Studies

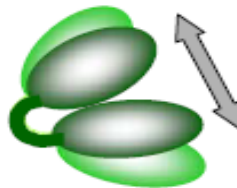
(From <http://www.embl.de/nmr/sattler/teaching>)



bond vibrations



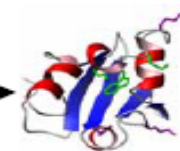
side chain rotations



domain movements



enzyme kinetics



folding, H/D exchange

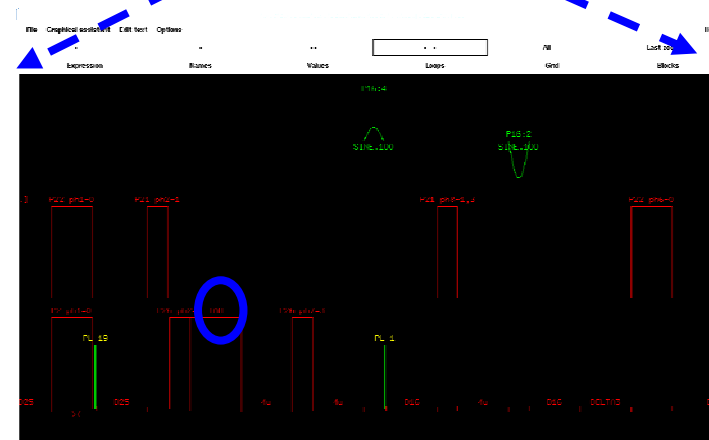
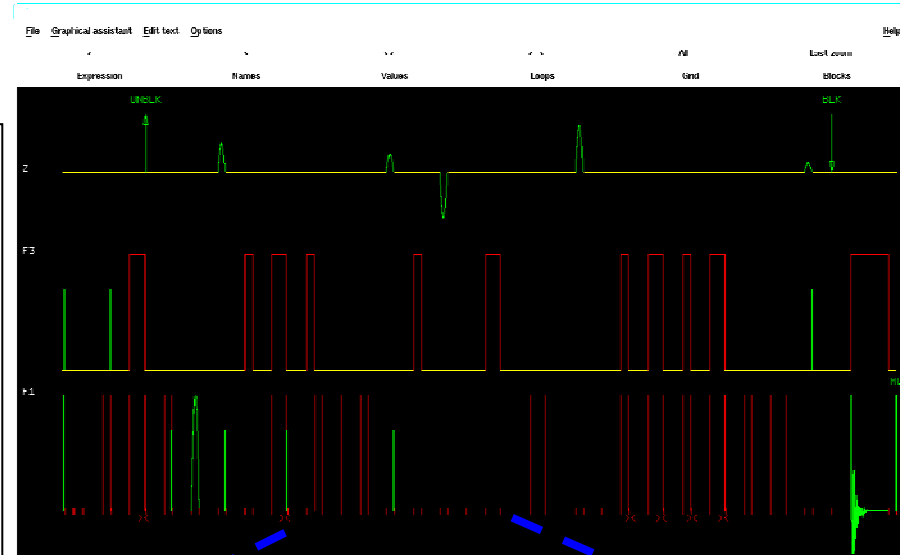
Part I. Study pico-sec to nano-sec motion

Step 1: Set up T1, T2, NOE Experiments

(1-1) T1 Experiment

<Option 1: Collect a series of 2D expts with different delay time>

- Experiment Type: `NHT1`
- Standard Parameter Set: `std1_2D_15N-T1_hsqct1etf3gpsi`
- Pulse Program: `hsqct1etf3gpsi`
- Easy Set Up Steps:
 - (1) `rpar std1_2D_15N-T1_hsqct1etf3gpsi`
 - (2) `getprosol 1H (us) (db)`
 - (3) `d7` : delay for inversion recovery in **sec** (different `d7` for different expts)
 - (4) `13C/15N sample: ZGOPTINS -DLABEL_CN`



(T1 delay → TAU value → d7)

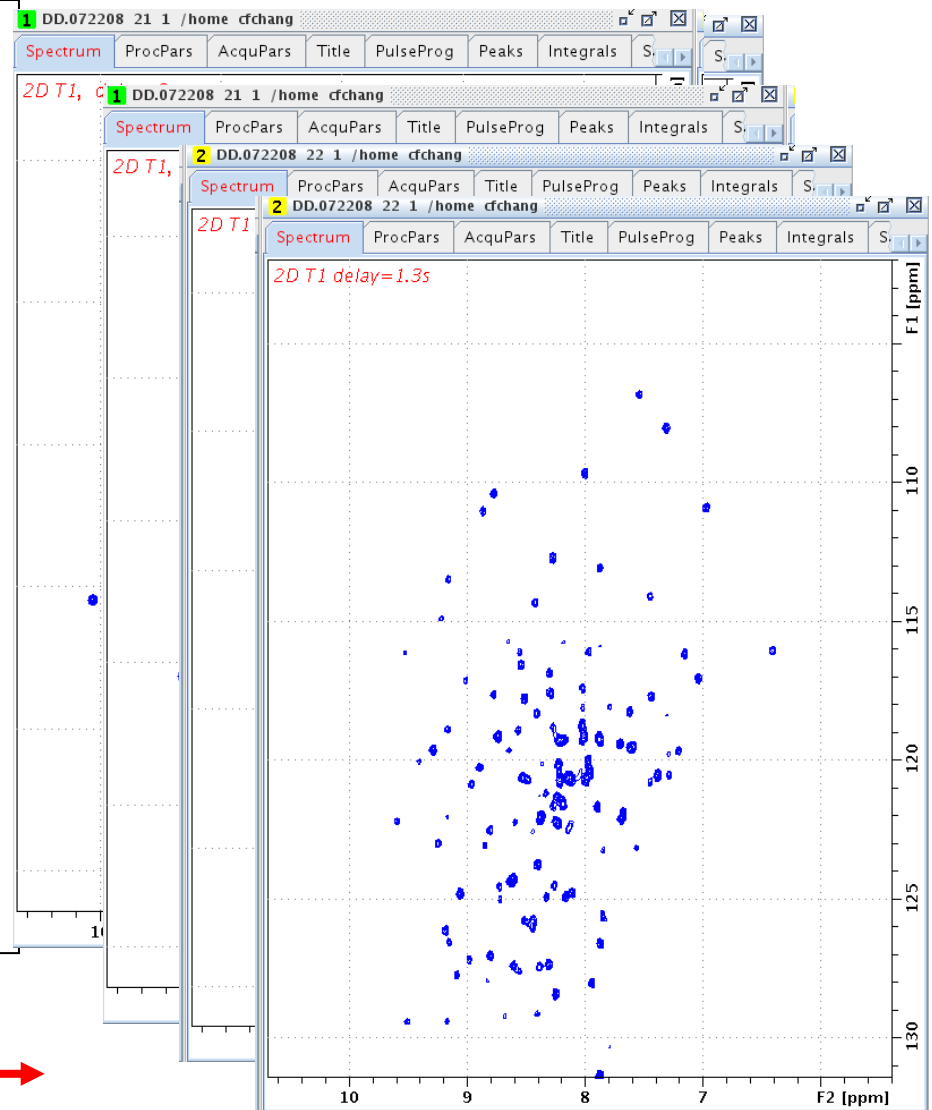
(1-1) T1 Experiment

<Option 2: Collect a set of pseudo 3D expt using vd-list for different delay time>

- Experiment Type: `NH T1 pseudo3D`
- Standard Parameter Set: `std1_3D_15N-T1_hsqct1etf3gpsi3d.2`
- Pulse Program: `hsqct1etf3gpsi3d.2`
- Easy Set Up Steps:
 - (1) `rpar std1_3D_15N-T1_hsqct1etf3gpsi3d.2`
 - (2) `getprosol 1H (us) (db)`
 - (3) edit `vd-list`: delay in **sec**, ex: `std_t1` (ex: `d7` in 2D version)
 - (4) NBL: number of delays in `vd-list`
 - (5) `td1`: number of delays in `vd-list` (QF)
 - (6) `13C/15N` sample: ZGOPTINS `-DLABEL_CN`



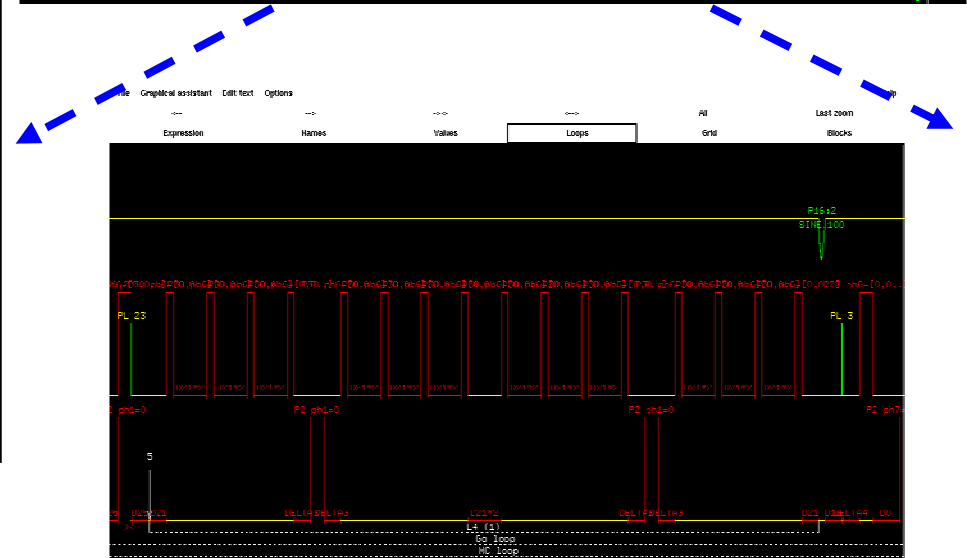
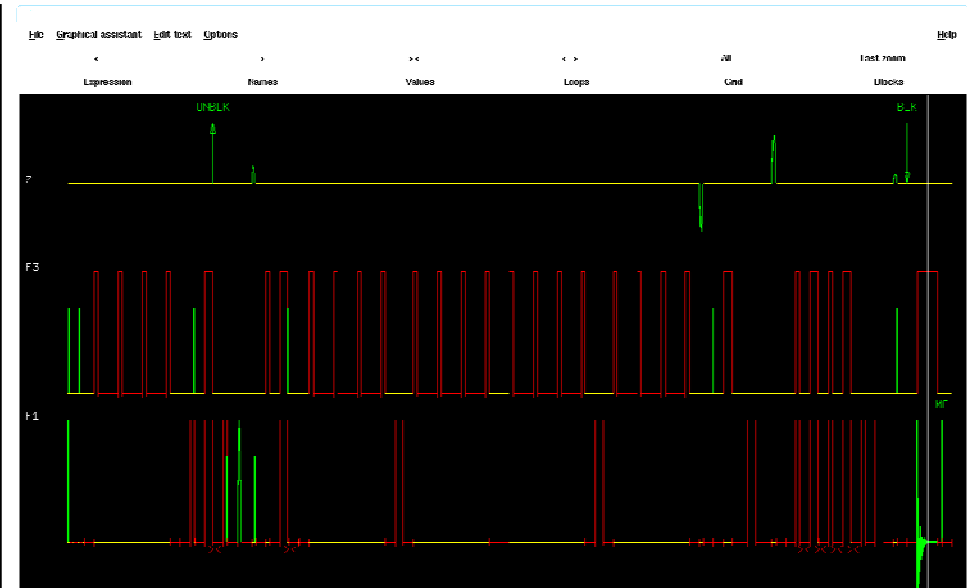
Increasing delays



(1-2) T2 Experiment

<Option 1: Collect a series of 2D expts with different delay time>

- Experiment Type: **NH T2**
- Standard Parameter Set: **std1_2D_15N-T2_hsqct2etf3gpsi**
- Pulse Program: **hsqct2etf3gpsi**
- Easy Set Up Steps:
 - (1) **par std1_2D_15N-T2_hsqct2etf3gpsi**
 - (2) **getprosol 1H (us) (db)**
 - (3) **d20 : T2 delay sec (different d20 for different expts)**
 - (4) **L5: loop for compensation for heating effects**
 - (5) **13C/15N sample: ZGOPTINS -DLABEL_CN**

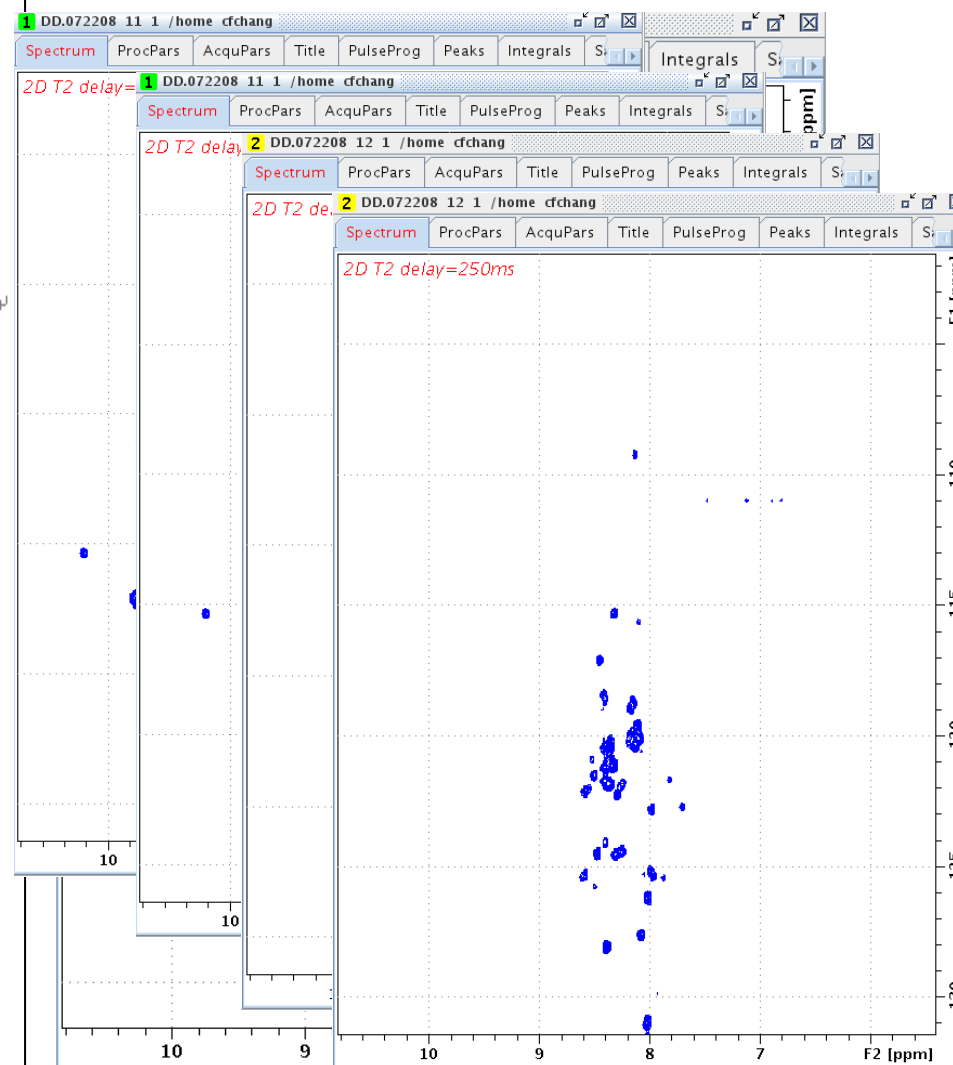


(T2 delay → loop number → d20)

(1-2) T2 Experiment

<Option 2: Collect a set of pseudo 3D expt using vc-list for different delay time>

- Experiment Type: **NH T2 pseudo3D**
- Standard Parameter Set: **std1_3D_15N-T2_hsqct2etf3gpsi3d**
- Pulse Program: **hsqct2etf3gpsi3d**
- Easy Set Up Steps:
 - (1) rpar **std1_3D_15N-T2_hsqct2etf3gpsi3d**
 - (2) getprosol **1H (us) (db)**
 - (3) edit vc-list: loop counter for T2 delay
(ex: $c=d20/(p30*16+d21*32)$ in 2D version)
 - (4) NBL: number of delays in vc-list
 - (5) td1: number of delays in vd-list (QF)
 - (6) 13C/15N sample: ZGOPTINS **-DLABEL_CN**



Increasing delays

(1-3) heteronuclear NOE Experiment

<Option : Collect an “interleave” expt for non-saturated and saturated spectra

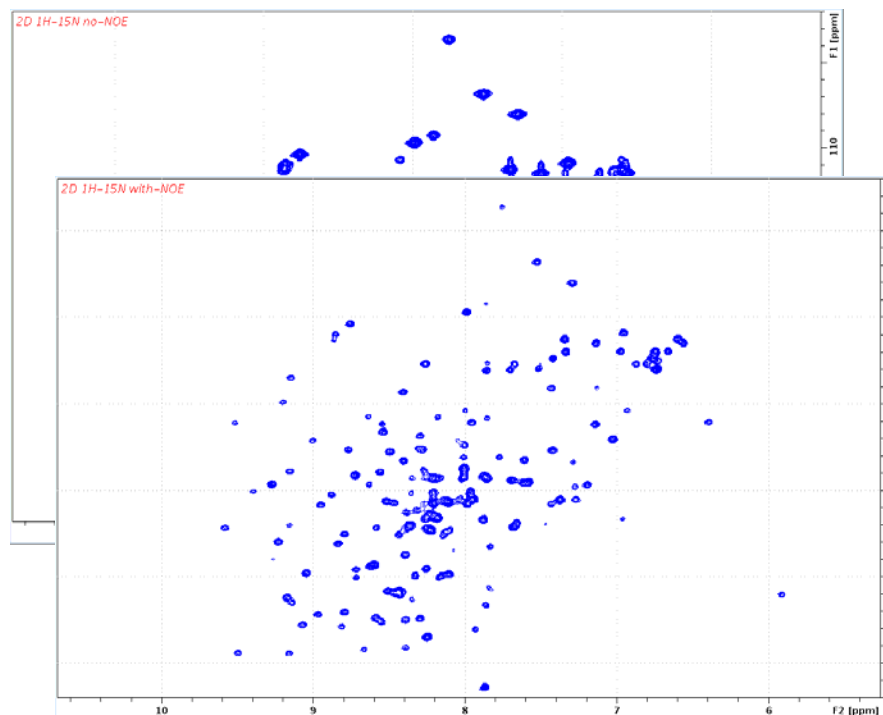
- ↵
- Experiment Type: **NH NOE** ↵
- Standard Parameter Set: **std1_2D_15N-NOE_hsqcnoef3gpsi** ↵
- Pulse Program: **hsqcnoef3gpsi** ↵

↵

● Easy Set Up Steps: ↵

- (1) rpar **std1_2D_15N-NOE_hsqcnoef3gpsi** ↵
- (2) getprosol **1H (us) (db)** ↵
- (3) D1 (ex: 5 sec) ↵
- (4) Note for process: xau **splitinvnoe** ↵

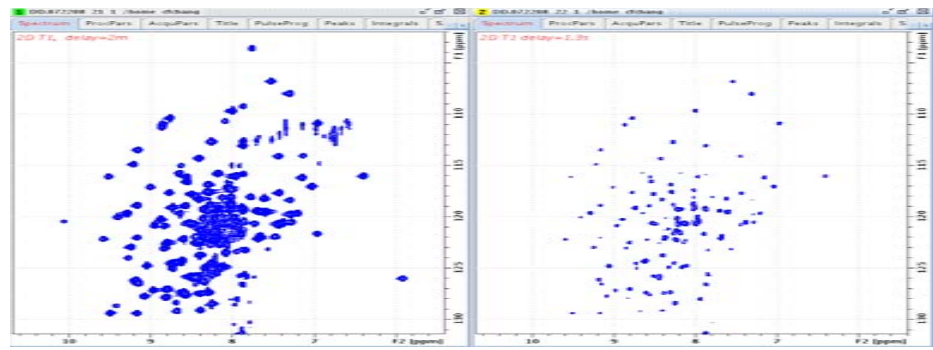
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Part I. Study pico-sec to nano-sec motion

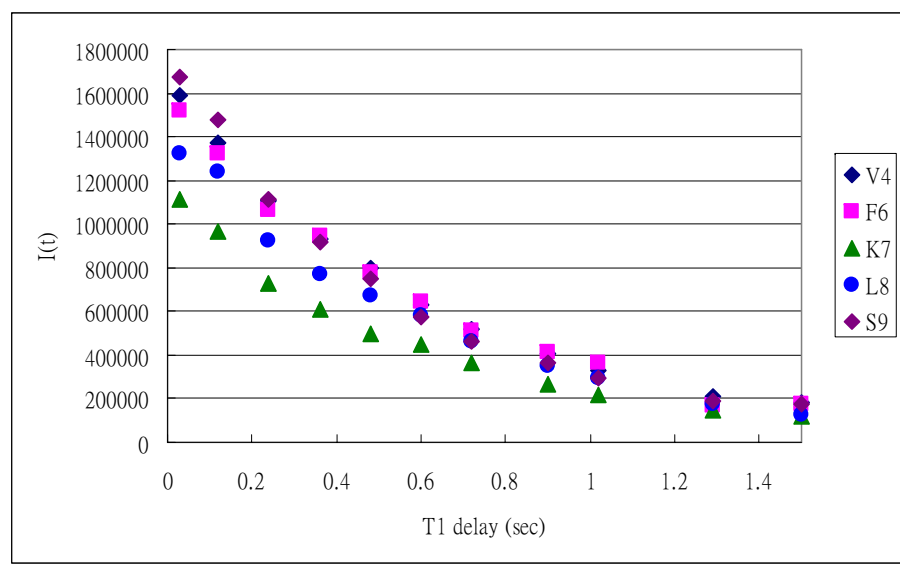
Step 2: Determine T1, T2, NOE Values for each residue

(2-1) T1 value from Curve Fitting



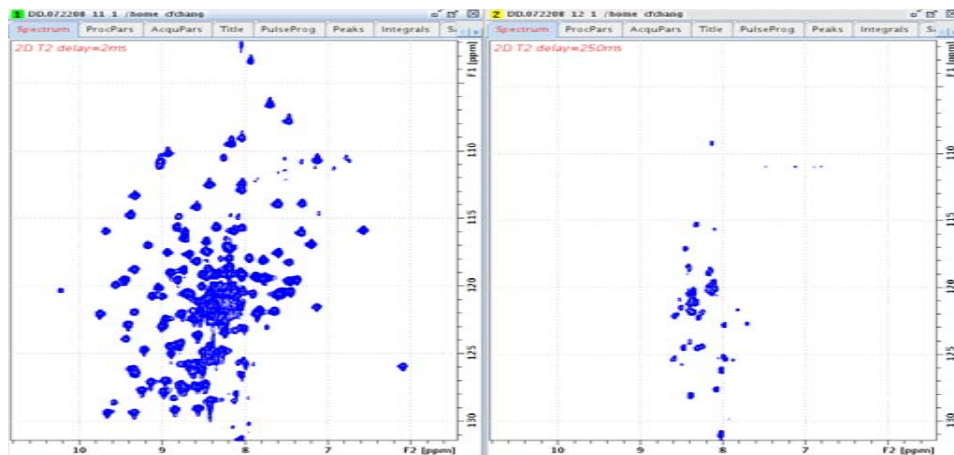
$$I(t) = I_0 \exp(-t/T_1)$$

$$R_1 = 1/T_1$$



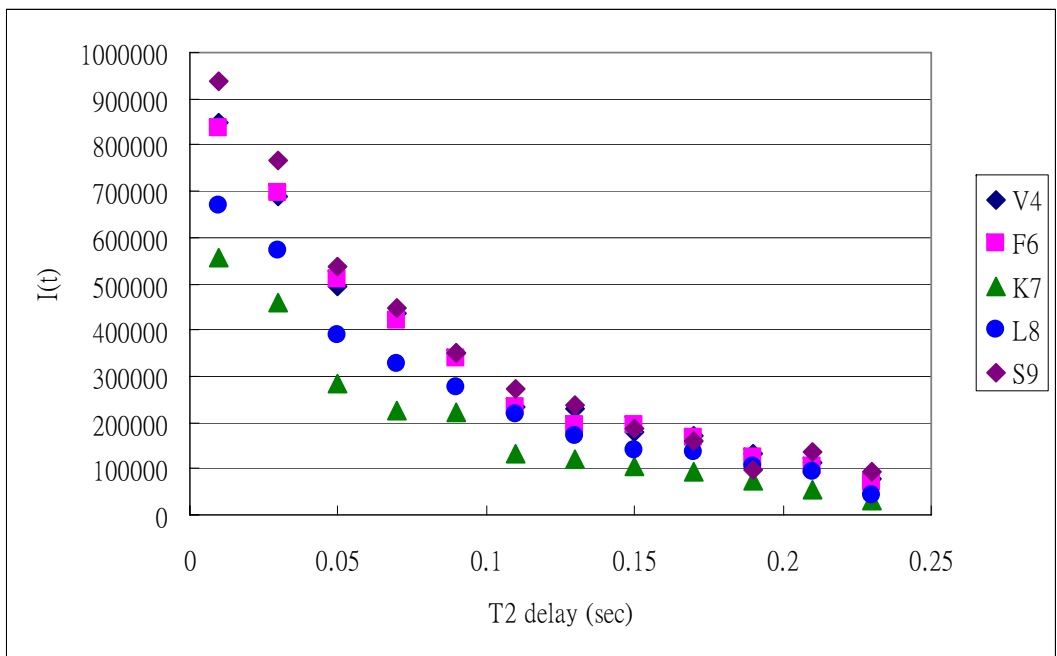
	R1	dR1	Goodness of Fit
V4	1.5876	0.022816	0.99891
F6	1.5273	0.038721	0.99658
K7	1.651	0.051077	0.99498
L8	1.5583	0.05192	0.99416
S9	1.8034	0.045471	0.99682

(2-2) T2 Value from Curve Fitting



$$I(t) = I_0 \exp(-t/T_2)$$

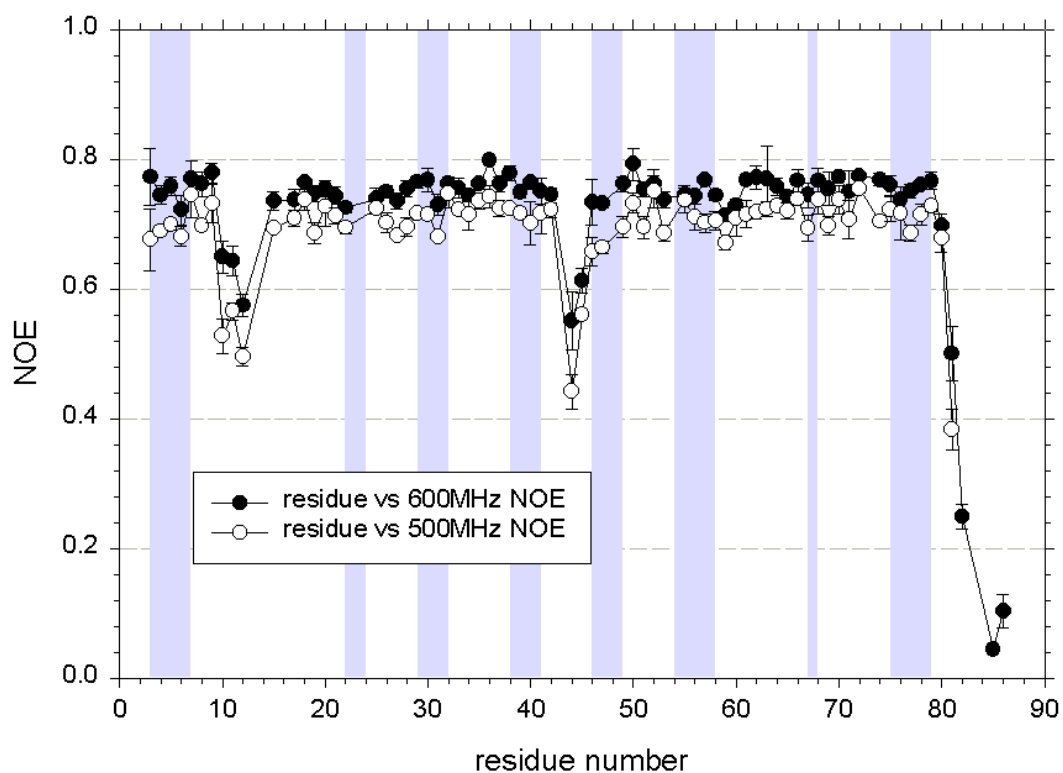
$$R_2 = 1/T_2$$



	R2	dR2	Goodness of Fit
V4	11.015	0.4209	0.99082
F6	11.274	0.39935	0.99225
K7	12.834	0.77788	0.97916
L8	11.122	0.4692	0.98897
S9	11.751	0.44541	0.99127

(2-3) heteronuclear NOE Values

NOE : intensity ratio ($I_{H,sat}/I_{un-sat}$)



	{noe}	STDEV
V4	0.743406	0.015822
F6	0.755803	0.027293
K7	0.768606	0.012184
L8	0.738638	0.033837
S9	0.761837	0.026417

Part I. Study pico-sec to nano-sec motion

Step 3: Dynamics Parameters from T1 (1/R1) , T2 (1/R2), NOE

(3-1) Reduced Spectral Density Mapping : $J(0.87\omega_H)$, $J(\omega_N)$, $J(0)$

From R1, R2, NOE values

$$\sigma_{NH} = R_1(\text{NOE}-1) (\gamma_H / \gamma_N)$$

$$J(0.87\omega_H) = 4 \sigma_{NH} / (5d^2)$$

$$J(\omega_N) = (4R_1 - 5 \sigma_{NH}) / (3d^2 + 4c^2)$$

$$J(0) = (6R_2 - 3R_1 - 2.72 \sigma_{NH}) / (3d^2 + 4c^2)$$

(Farrow et al, 1995)

Reduced
Spectral density
function mapping

Obtain parameter $J(0)$, $J(\omega_N)$, $J(0.87\omega_H)$, S^2 , τ_μ and R_{ex} for each residue

- $J(0)$, $J(\omega_N)$ decrease: Greater internal motion
- $J(0.87\omega_H)$ increase: Greater internal motion
- Significantly increased $J(0)$: Chemical exchange

(3-2) Model Free Analysis: S^2 , τ , R_{ex}

From R_1 , R_2 , NOE values to Spectral Density Function

$$R_1 = (d^2/4)[J(\omega_H - \omega_N) + 3J(\omega_N) + 6J(\omega_H + \omega_N)] + c^2 J(\omega_N)$$

$$R_2 = (d^2/8)[4J(0) + J(\omega_H - \omega_N) + 3J(\omega_N) + 6J(\omega_H) + 6J(\omega_H + \omega_N)] + (c^2/6)[4J(0) + 3J(\omega_N)] + R_{ex}$$

$$NOE = 1 + (d^2/4R_1)(\gamma_H/\gamma_N) + [6J(\omega_H + \omega_N) - J(\omega_H - \omega_N)]$$

in which $d = \mu_0 h \gamma_X \gamma_H \langle r_{XH}^{-3} \rangle / (8\pi^2)$, $c = \omega_X \Delta\sigma / \sqrt{3}$, μ_0 is the permeability of free space; h is Planck's constant; γ_H and γ_X are the gyromagnetic ratios of 1H and the X spin ($X = ^{13}C$ or ^{15}N), respectively; r_{XH} is the X-H bond length; ω_H and ω_X are the Larmor frequencies of 1H and X spins, respectively; and $\Delta\sigma$ is the chemical shift anisotropy of the X spin (assuming an axially

(Clare et al., 1990)

From Spectral Density Function $J(\omega)$ to dynamics parameters

$$J(\omega) = \frac{2}{5} \left[\frac{S^2 \tau_m}{1 + (\omega \tau_m)^2} + \frac{(S_f^2 - S_s^2) \tau}{1 + (\omega \tau)^2} \right]$$

$$= \frac{2}{5} S_f^2 \left[\frac{S_s^2 \tau_m}{1 + (\omega \tau_m)^2} + \frac{(1 - S_s^2) \tau}{1 + (\omega \tau)^2} \right]$$

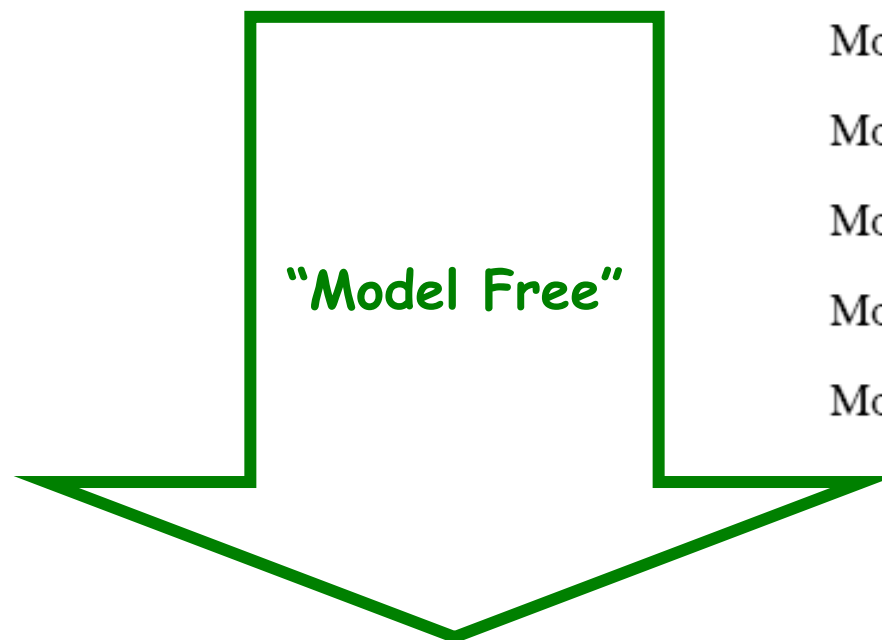
$$S^2 = S_f^2 S_s^2$$

$$\tau = \tau_s \tau_m / (\tau_s + \tau_m)$$

in which $\tau = \tau_s \tau_m / (\tau_s + \tau_m)$, τ_m is the isotropic rotational correlation time of the molecule, τ_s is the effective correlation time for internal motions, $S^2 = S_f^2 S_s^2$ is the square of the generalized order parameter characterizing the amplitude of the internal motions, and S_f^2 and S_s^2 are the squares of the order parameters for the internal motions on the fast and slow time scales, respectively. Generalized

(3-2) Model Free Analysis: S^2 , τ , R_{ex}

From R_1 , R_2 , NOE values, and based on Spectral Density Function $J(\omega)$



Model 1: S^2 s

Model 2: S^2 s and τ_e

Model 3: S^2 s and R_{ex}

Model 4: S^2 s, τ_e and R_{ex}

Model 5: S_f^2 , S_s^2 , and τ_e

Obtain parameter S^2 , τ and R_{ex} for each residue



- Order parameter, S^2 : Degree of internal motion
- Correlation time, τ : Rate of molecule motion
- Exchange rate, R_{ex} : Conformational exchange

Part I. Study pico-sec to nano-sec motion

Collect T1, T2, NOE

- Curve Fitting to Obtain T1, T2 values
- Intensity Ratio to obtain NOE values

Sparky, CCPN,
Topspin, Excel,
Others.....

Mapsdf_new_Mar00

Reduced Spectral
Density Function

$J(0), J(\omega_N), J(0.87\omega_H)$
 τ_m, S^2

pico-sec to nano-sec
motion

$R2/R1 \rightarrow \tau_m$

R2R1_TM

Model-Free Analysis

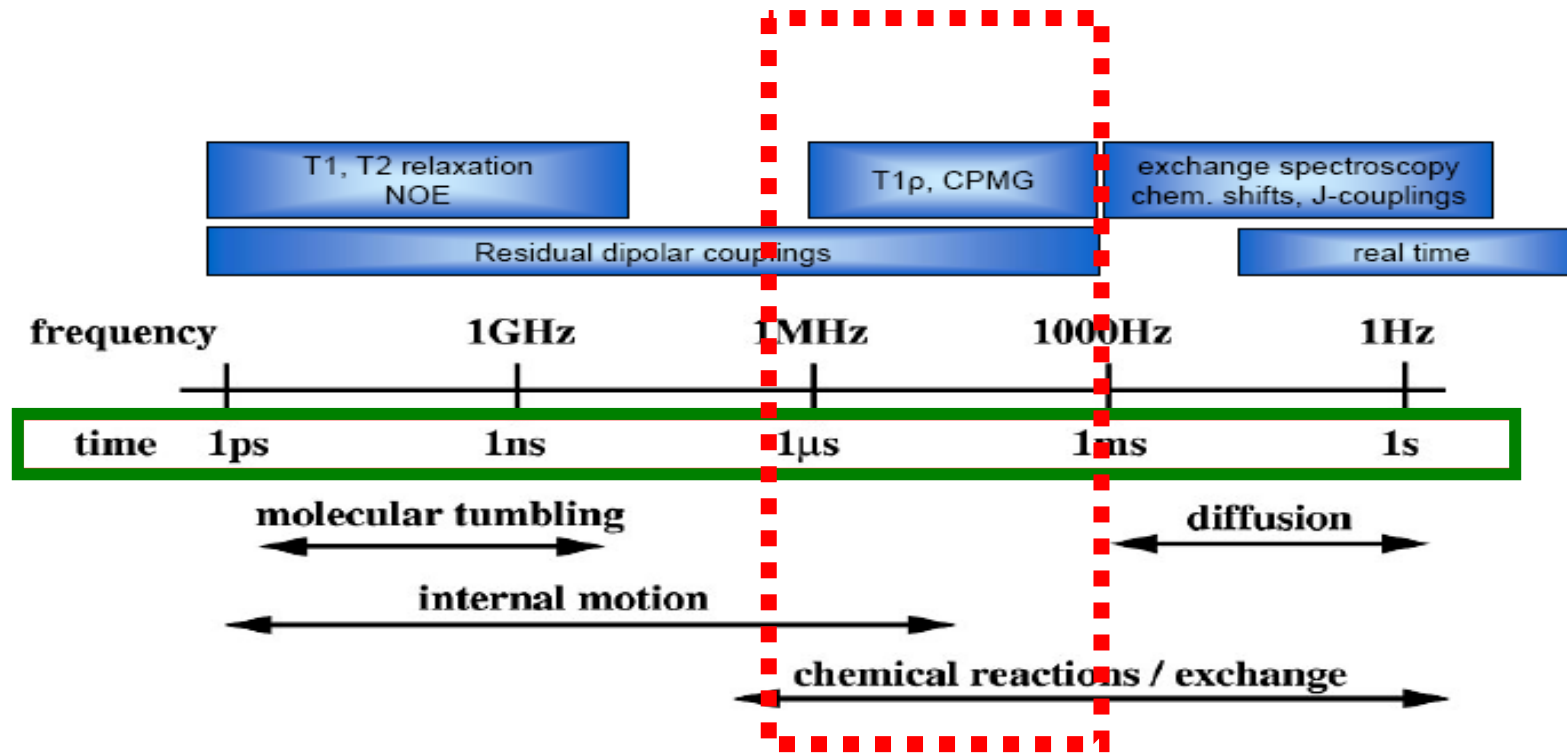
Quadric_Diffsuion
Model-Free

τ_e, R_{ex}, S^2

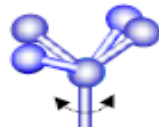
pico-sec to nano-sec
motion

NMR Time Scales for Protein Dynamics Studies

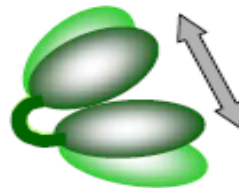
(From <http://www.embl.de/nmr/sattler/teaching>)



bond vibrations



side chain rotations



domain movements



enzyme kinetics



folding, H/D exchange

Note on relaxation dispersion

- Relaxation dispersion monitor dynamics on the range of **us to ms (10^{-6} to 10^{-3})**.
- Relaxation dispersion can separate the contribution from exchange between different conformations (**Rex**) from total R2 relaxation
- **Rex** is a function of **exchange rates, populations and chemical shifts** of the different conformations. Thus, give information on the kinetics, thermodynamics, as well as structure of protein substrates. Folding intermediates can be detected as well.
- Parameters that characterize the kinetics of the chemical exchange process are obtained from the variation of **R1rho as a function of ω_e** (effective field in the rotation frame), called **relaxation dispersion**.
- **CPMG** relaxation experiments monitor the decay of transverse magnetization in a series of spin-echo pulse sequence elements. Chemical exchange is characterized from the variation in the transverse relaxation rate constant, **R2, as a function of the time delay τ_{cp}** . Where an effective field strength for the CPMG experiment can be defined as $\omega_{cpmg} = 12^{1/2} / \tau_{cp}$

Part II. Study micro-sec to milli-sec motion

Method 1: R1rho relaxation Dispersion Experiments (μs)

(1-1) R1rho Experiment

<Collect a set of pseudo 3D expt using vd-list for different field>

- Experiment Type: NH HSQC type pseudo3D
- Standard Parameter Set: std1_3D_15N-R1rho_hsqctretf3gpsi3d.2
- Pulse Program: hsqctretf3gpsi3d.2
- Reference: JACS, 124,10743 (2002)

↵

- Easy Set Up Steps:

↵

- (1) rpar std1_3D_15N-R1rho_hsqctretf3gpsi3d.2
- (2) getprosol 1H (us) (db)
- (3) edit vd-list: delay in sec, ex: std_t1rho
- (4) NBL: number of delays in vd-list
- (5) td1: number of delays in vd-list (QF)
- (6) 13C/15N sample: ZGOPTINS -DLABEL_CN

(1-2) Determine Kex from R1rho experiment

$$R_{\text{ex}} = k_{\text{ex}} \Phi_{\text{ex}} / (k_{\text{ex}}^2 + \omega_e^2)$$

$$R_{1\rho} = R_1 \cos^2 \theta + R_2^0 \sin^2 \theta + \frac{\varphi_{\text{ex}} k_{\text{ex}}}{k_{\text{ex}}^2 + \omega_e^2} \sin^2 \theta$$

$$\theta = \arctan(\omega_1 / \Omega)$$

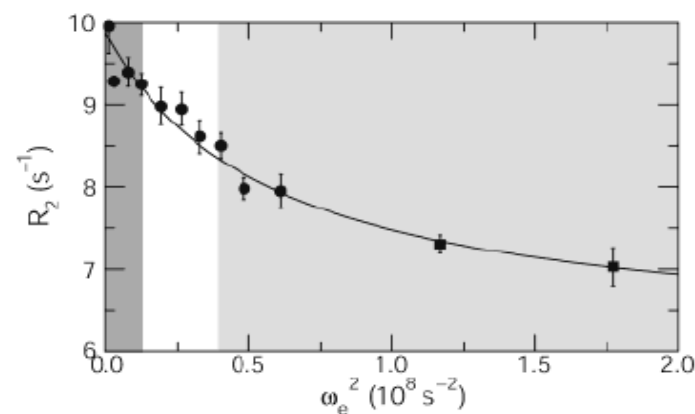
Ω : Resonance offset from the spin-lock frequency

ω_1 : amplitude of the spin-lock field

$\omega_e = (\omega_1^2 + \Omega^2)^{1/2}$: effective spin-lock field

$\varphi_{\text{ex}} : p_A p_B \Delta \omega^2$

$$R_2 = \frac{\varphi_{\text{ex}} k_{\text{ex}}}{k_{\text{ex}}^2 + \omega_e^2} + R_2^0$$



(Loria et al., Accounts of Chemical Research, 214-221, 2008)

Method 2: CPMG relaxation Dispersion Experiments (ms)

(2-1) CPMG Experiment

<Collect a set of pseudo 3D expt using vd-list for τ_{cp} >

- Experiment Type: NH TROSY type pseudo3D
- Standard Parameter Set: std2_3D_15N-T2Rex_trrexetf3gpsi3d_3.cf
- Pulse Program: trrexetf3gpsi3d_3.cf
- Reference: JACS 130, 2432-3 (2008)

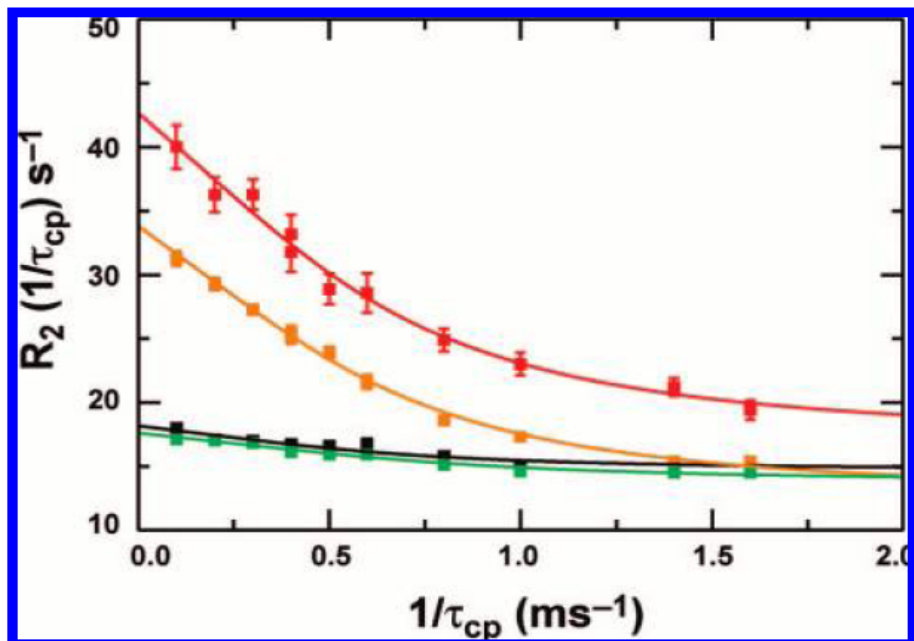
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- Easy Set Up Steps:

↵

- (1) rpar std2_3D_15N-T2Rex_trrexetf3gpsi3d_3.cf
- (2) getprosol 1H (us) (db)
- (3) edit vd-list : field strength in Hz, ex: std_Rex
- (4) NBL: number of delays in vd-list
- (5) td1: number of delays in vd-list (QF)
- (6) decide d21 value: length of mixing time , ex: 25ms
- (7) 13C/15N sample: ZGOPTINS -DLABEL_CN
- (8) d1=2.5sec

(2-2) Determine k_{ex} from CPMG experiment

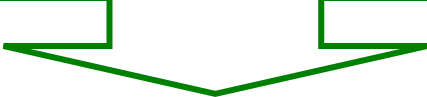


$$R_2(1/\tau_{cp}) = R_2^0 + \varphi_{ex} k_{ex} [1 - 2 \tanh(k_{ex} \tau_{cp}/2) / (k_{ex} \tau_{cp})]$$

$$\omega_e = 12^{1/2} / \tau_{cp}$$

Part II. Study micro-sec to milli-sec motion

Collect R1rho, CPMG
Relaxation Dispersion
Experiments



Curve Fitting to obtain Kex value

Sparky, CCPN,
Topspin, Excel,
Others.....



Rex



micro-sec to milli-sec
motion

Now,

Let's See how

"Protein Dynamics Center"

Could help?